

The Size-Power Tradeoff in HAR Inference: Supplement

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This supplement provides additional figures and Monte Carlo results.

Figure S.1 plots the implied mean kernel for the Fourier, cosine, Legendre, and SS basis functions for $B = 8$ and $T = 200$. The Fourier transforms of these implied mean kernels, that is, the frequency-domain implied mean kernel, are plotted in Figure S.2 at the frequencies $2\pi j/T$, $j = 1, \dots, 32$. The EWP (Fourier) estimator is the only one of these four that has an exact kernel representation, and its frequency-domain kernel is the familiar flat (Daniell) kernel that gives equal weight to the first $B/2$ periodogram ordinates. The remaining three implied mean kernels in the frequency domain also concentrate their mass at low frequencies.

Figure S.3 shows the power difference, as a function of the standardized local alternative δ , between the EWP and QS test, for $B = 8$ for EWP and b for QS chosen so that the two tests have the same size-adjusted power. This curve is computed using the expression in Theorem 3 and Remark 6.

Figure S.4 shows additional Monte Carlo results for different values of T for 6 tests: QS, EWP, Cos (type II cosine basis function), NW, Legendre basis function, and SS.

Figure S.5 shows the spectral density for the AMA(2,1) process. The parameters are calibrated so that $\omega^{(2)} = 4$ and with a spectral density approximately symmetric around $\pi/2$, with a minimum at $\pi/2$ (the coefficients are $\rho_1 = 0.048$, $\rho_2 = 0.248$, $\theta = -0.064$).

Figure S.6 shows results for the ARMA(2,1) disturbances, $m = 1$.

Figures S.7 and S.8 show additional results for $m = 2$.

Figure S.9 shows results in the location model, feasible higher-order corrected critical values, ARMA(2,1) errors.

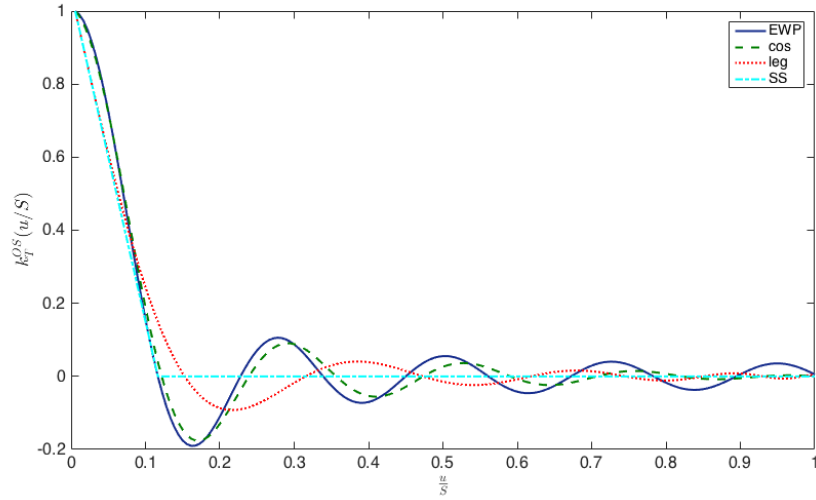


Figure S.1. Implied mean kernel of basis function estimators with $B = 8$, time domain: Fourier/EWP (dark blue, solid), cosine (light blue, dash), Legendre (red, dot), and split-sample (teal, dash-dot).

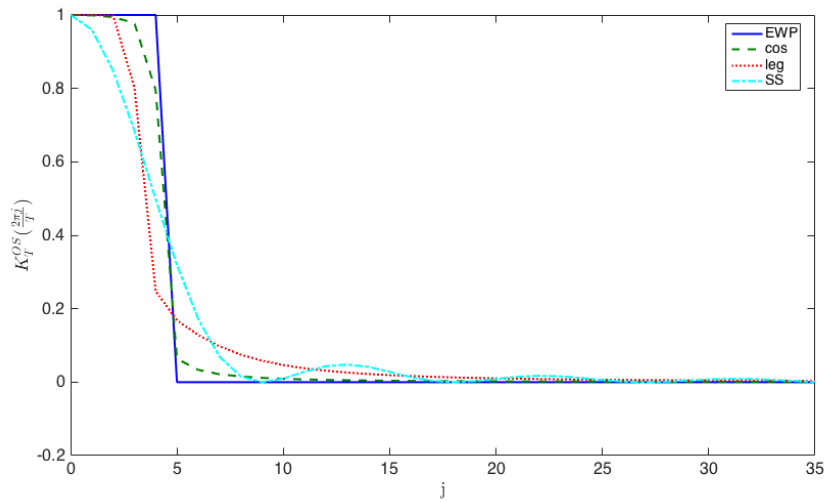


Figure S.2. Implied mean kernel of basis function estimators with $B = 8$, frequency domain: Fourier/EWP (dark blue, solid), cosine (light blue, dash), Legendre (red, dot), and split-sample (teal, dash-dot). The frequency domain kernel is normalized to 1 at $\omega = 0$ and computed over the periodogram ordinates (so the horizontal axis value j corresponds to $2\pi j/T$, etc.)

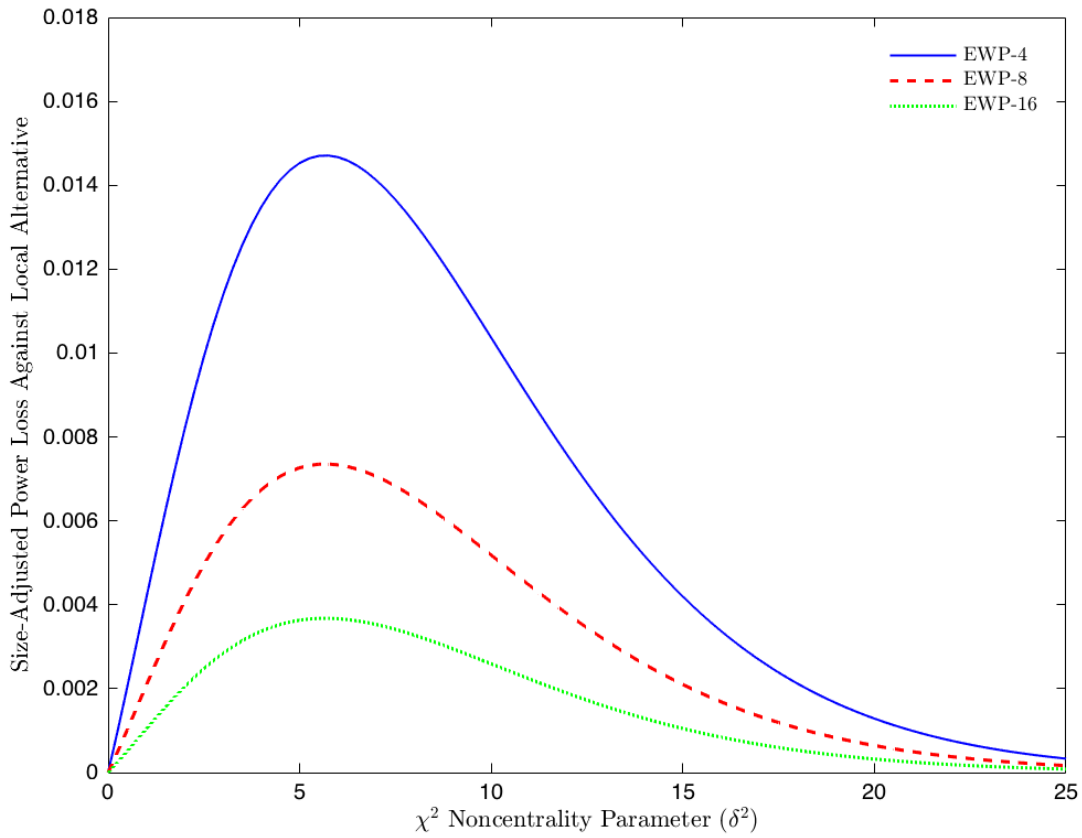


Figure S.3. Small- b approximation to power loss for EWP test, compared to QS test, for different values of B in the EWP test and with b for the QS test chosen so that the EWP and QS test have the same higher-order size when evaluated using fixed- b critical values. The figure plots the final expression in (45) as a function of δ . Gaussian location model, $m=1$, 5% significance level.

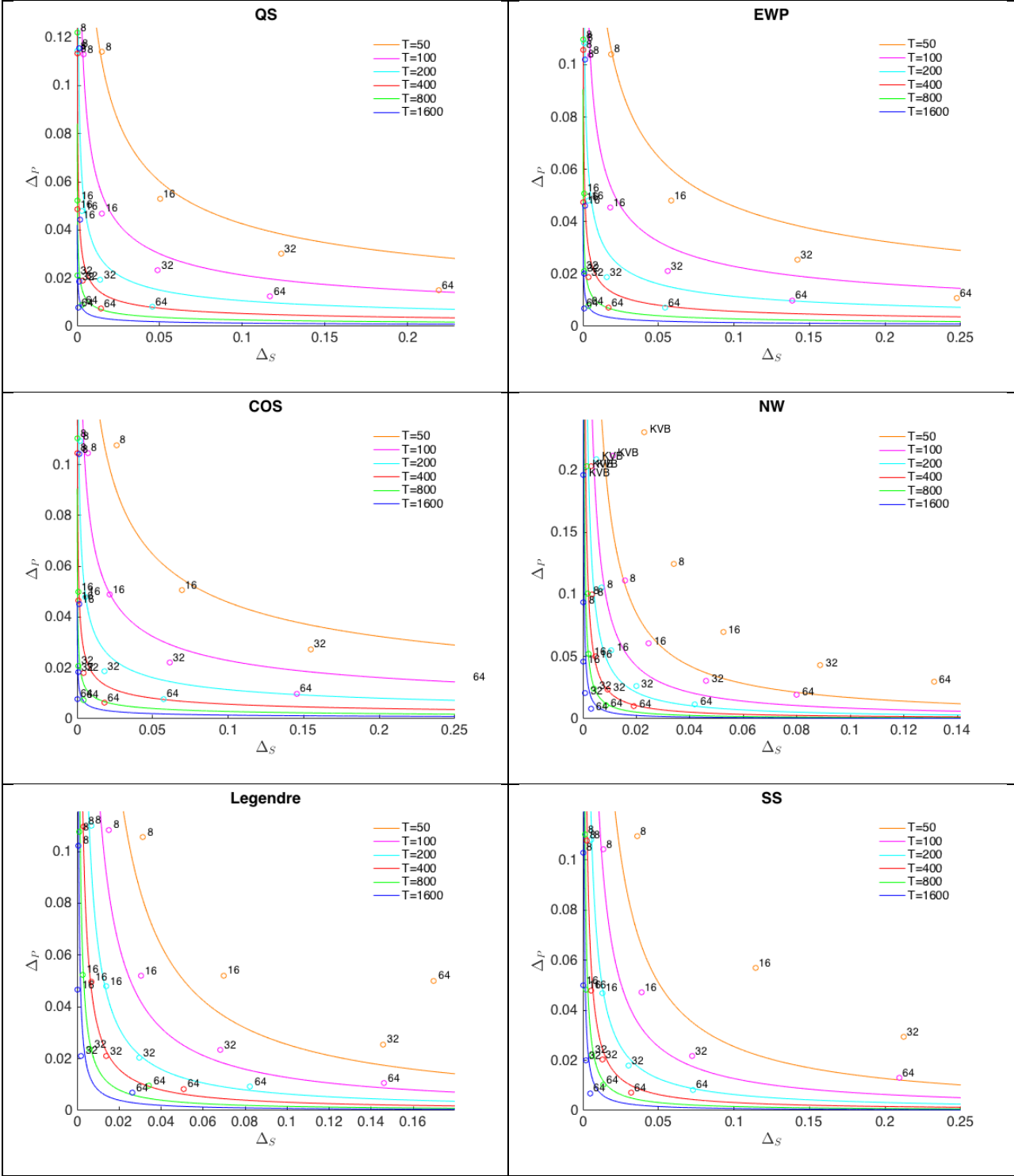


Figure S.4. Location model, AR(1), $m = 1$, $\rho = 0.5$
 Theoretical size distortion/power loss trade-off curves for each estimator with Monte Carlo results for T ranging from 50 to 1600.

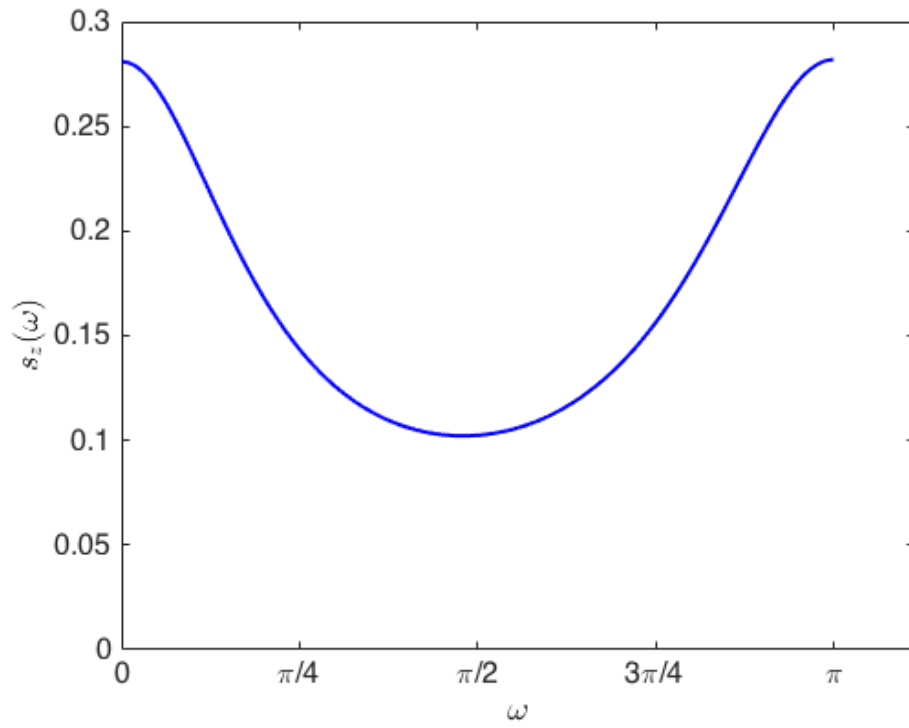


Figure S.5. Spectral density of calibrated ARMA(2,1), $\omega^{(2)} = 4$

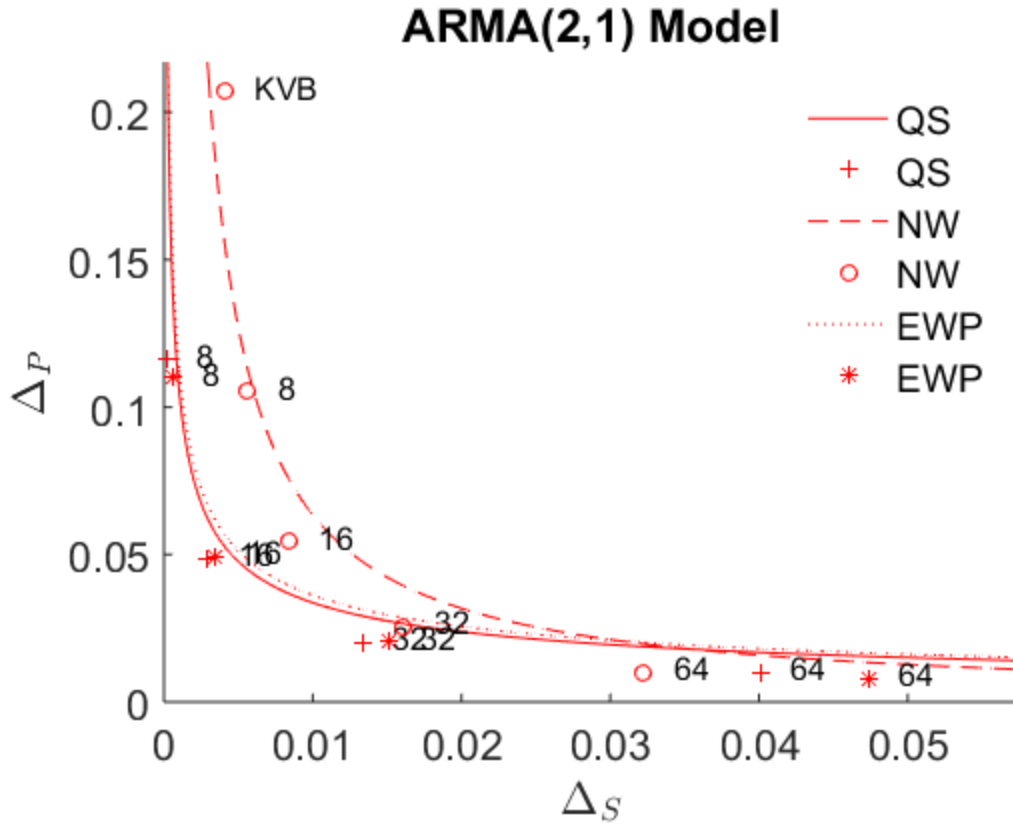


Figure S.6. Location model, ARMA(2,1), $m = 1$, $T = 200$
 Theoretical size distortion/power loss trade-off curves for QS, Newey-West, and EWP estimators with Monte Carlo results. ARMA(2,1) parameters fixed such that $\omega^{(2)} = 4$, equivalent to AR(1) with $\alpha = 0.5$ (parameter values as in Figure S.5)

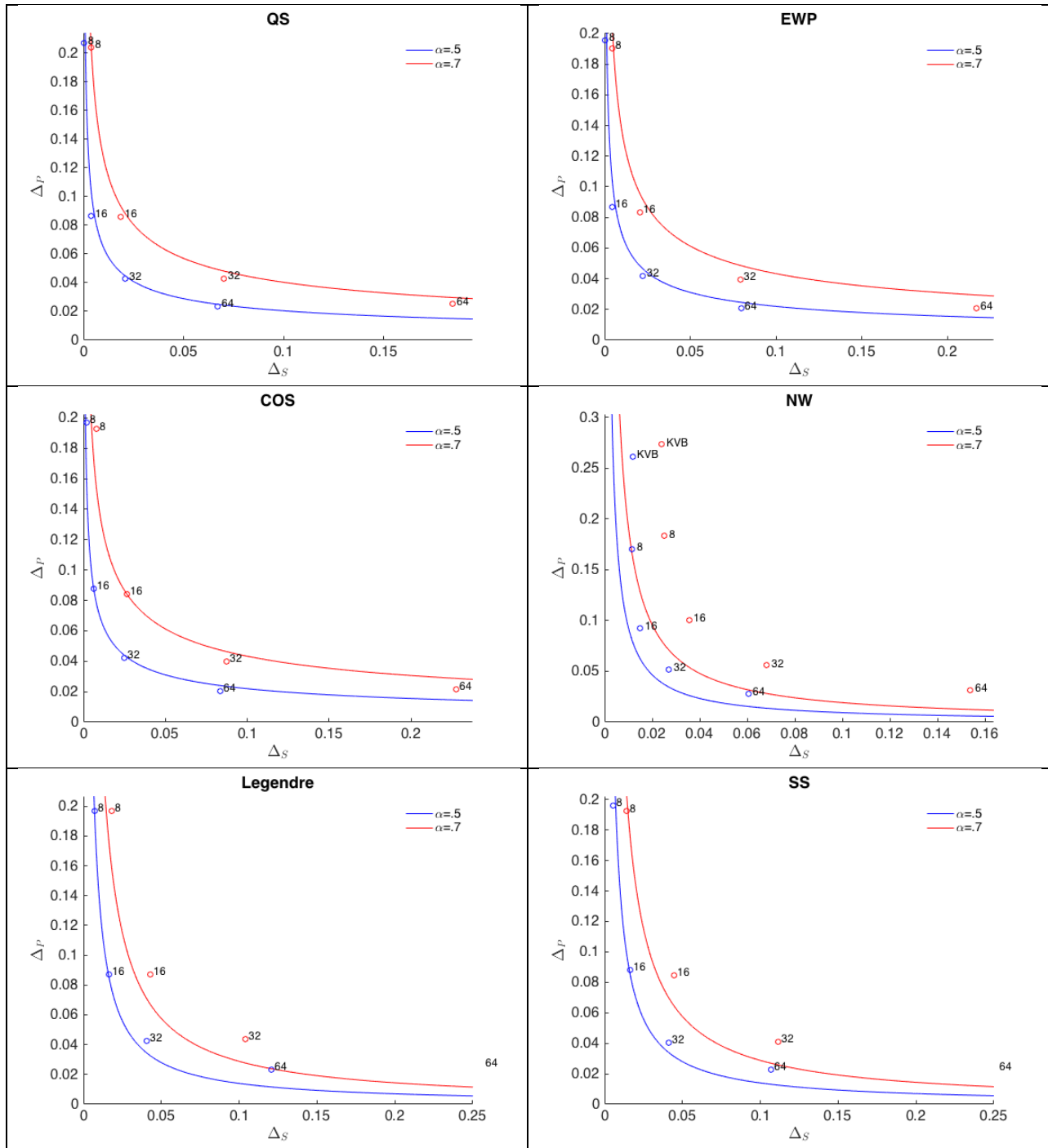


Figure S.7. Location model, AR(1), $m = 2$, $\rho = .5$ and $.7$, $T = 200$
 Theoretical size distortion/power loss trade-off curves for each estimator and Monte Carlo results (dots)

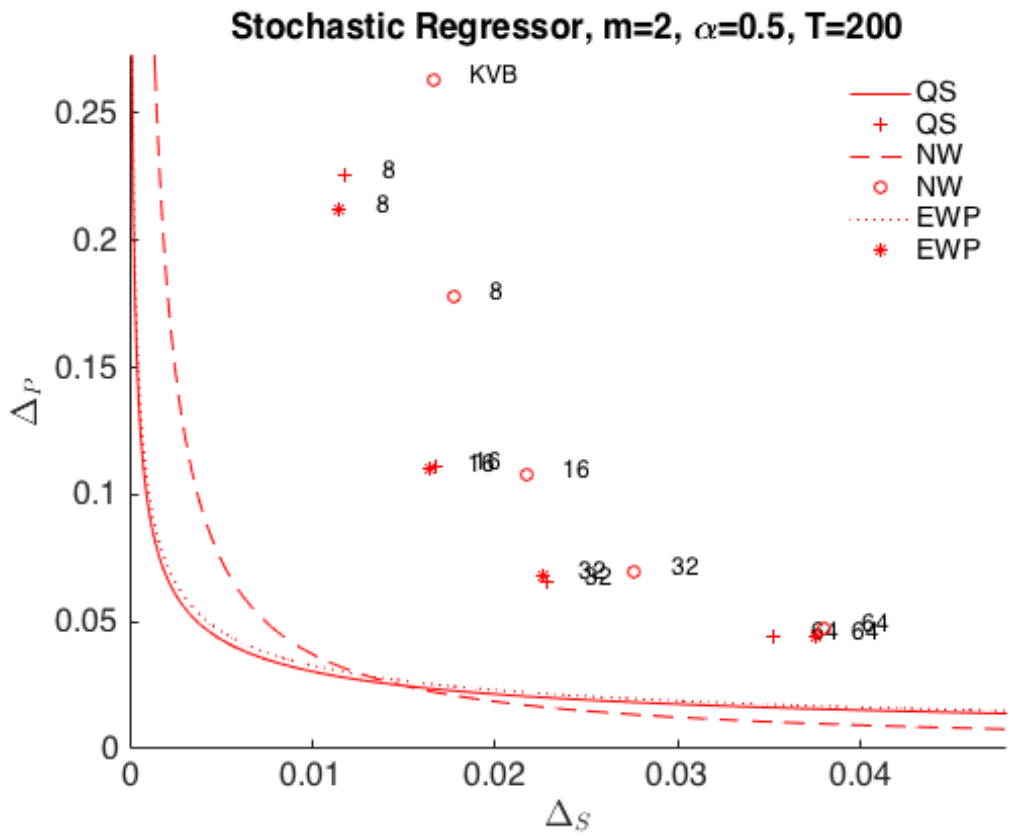


Figure S.8. Stochastic regressor, AR(1), $m = 2, \rho = 0.5, T = 200$
 Theoretical size distortion/power loss trade-off curves for QS, Newey-West, and EWP estimators with Monte Carlo results. *Note:* curves are for the Gaussian location model.

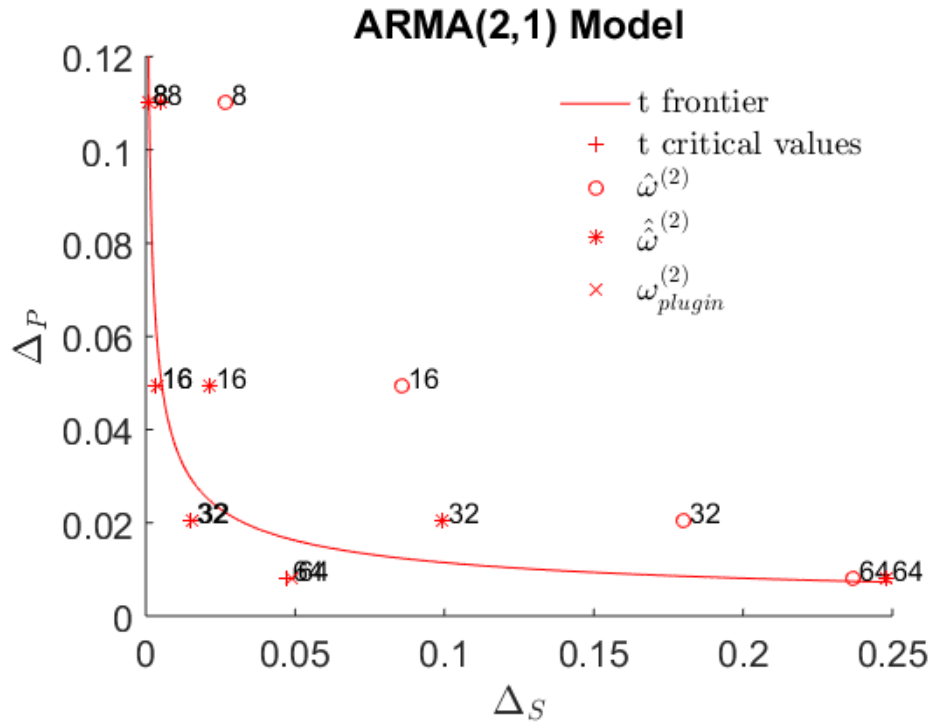


Figure S.9. Theoretical (lines) and Monte Carlo (symbols) size distortion/power loss curves for the EWP estimator using feasible higher-order adjusted critical values: Location model, $m = 1$, ARMA(2,1), parameter values as in Figure S.5, $T = 200$.